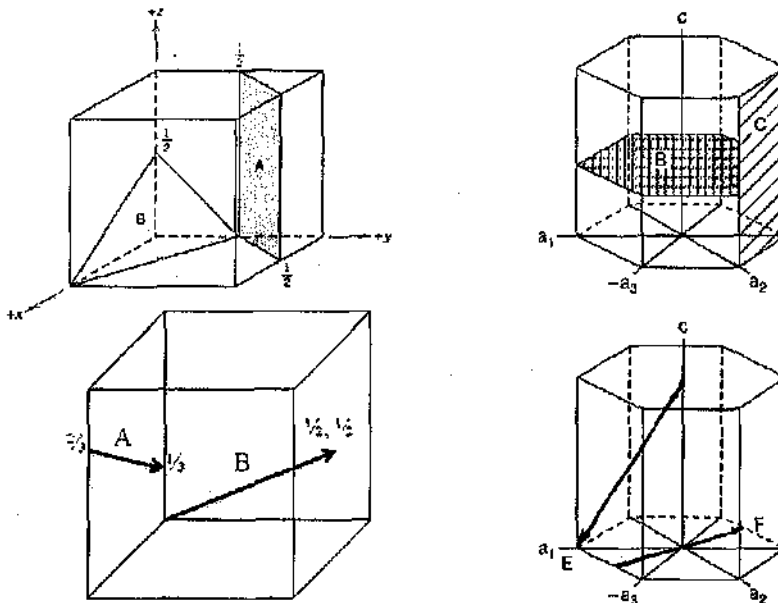


Instructions:

- Attempt ANY FOUR (4).
- Show your working and reasoning carefully for credit. Draw schematic diagrams wherever necessary.
- Points for each question are written below.
- Closed books, closed notes, closed laptop and cell phones. A calculator is allowed only.

1. (a) Determine the Miller indices of the following planes and directions:



(b) What is the fractional volume change in iron as it transforms from γ ($a = 0.365 \text{ nm}$) to δ ($a = 0.293$) at 1394°C ? What is the volume change if Fe atoms of fixed radius pack as hard spheres?

(c) Atoms of a body-centered tetragonal metal are arranged in a square array on the (001) plane with a lattice constant of 0.460 nm . On the (100) and (010) planes, atoms are arranged in a rectangular array with lattice constants of 0.460 and 0.495 nm . Sketch the atomic positions on the (110) plane and indicate the dimensions.

8 + 4 + 3 = 15

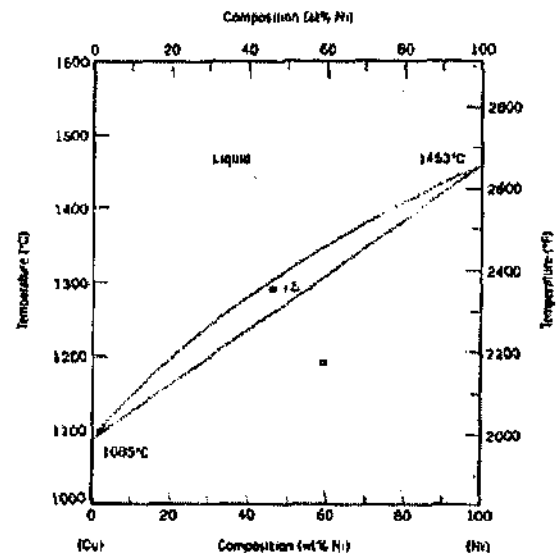
2. (a) Why polymers show high degree of deformation although they have primary covalent bonding?
- (b) Differentiate between resilience and toughness.
- (c) What is slip system? Why deformation in FCC metals is greater than BCC metals although BCC has more slip system than FCC?
- (d) Describe the microstructural features developed in a casting process.
- (e) Compute the number of atoms/ m^3 in pure Fe. Density of Fe = 7.8 g/cm^3 ; $A(\text{Fe}) = 55.85$; $Z(\text{Fe}) = 26$; Crystal Structure = BCC

- (f) Considering both temperature and pressure to be variables, what is the largest number of phases that can coexist at equilibrium in a binary alloy?
- (g) Briefly explain why a proeutectoid phase (ferrite or cementite) forms along austenite grain boundaries.

$$2 + 2 + 3 + 2 + 2 + 2 + 2 = 15$$

3. (a) Use the following diagram to answer the questions below:
A copper-nickel alloy of composition 70 wt% Cu is slowly cooled from a temperature of 1300°C.

- At what temperature does the first phase change will occur?
- What are the compositions of these liquid and solid phases?
- At what temperature does complete solidification of the alloy occur?
- What is the composition of the last liquid remaining prior to complete solidification?



- (b) Cite and identify the following position(s) of defect(s) with a vertical dashed line:

-ABABBBABA....
-ABABABBABAABABAB.....
-ABCABABCABC.....

- (c) In the table (next page), atomic radius, crystal structure, electronegativity, and the most common valence are tabulated for several elements; for those that are nonmetals, only atomic radii are indicated. Which of these elements would you expect to form the following with nickel:

- a substitutional solid solution having complete solubility?
- a substitutional solid solution of incomplete solubility?
- an interstitial solid solution?

Justify your answer.

Element	Atomic Radius (nm)	Crystal Structure	Electronegativity	Valence
Ni	0.1246	FCC	1.8	+2
C	0.071			
O	0.060			
Ag	0.1445	FCC	1.9	+1
Al	0.1431	FCC	1.5	+3
Cr	0.1249	BCC	1.6	+3
Fe	0.1241	BCC	1.8	+2
Cu	0.1278	FCC	1.9	+2
Pd	0.1376	FCC	2.2	+2
Zn	0.1332	HCP	1.6	+2

- (d) For an FCC single crystal, would you expect the surface energy for a (100) plane to be greater or less than that for a (111) plane? Explain.

$$4 + 3 + 6 + 2 = 15$$

4. (a) Consider a single crystal of nickel oriented such that a tensile stress is applied along a [001] direction. If slip occurs on a (111) plane and in a [101] direction, and is initiated at an applied tensile stress of 13.9 MPa, compute the critical resolved shear stress.

Given: An angle between directions, θ can be expressed as

$$\theta = \cos^{-1} \left[\frac{u_1 u_2 + v_1 v_2 + w_1 w_2}{\sqrt{(u_1^2 + v_1^2 + w_1^2)(u_2^2 + v_2^2 + w_2^2)}} \right]$$

[Hint: For cubic crystals, planes and directions having the same indices are perpendicular to one another.]

- (b) If the true-stress–true-strain curve is given by $\sigma = 1400e^{0.33}$, where stress is in MPa, determine the ultimate tensile strength of the material.

[Given: Uniform elongation at maximum load is $\epsilon = n$; engineering stress, $s = \sigma/(e + 1)$; true strain, $\epsilon = \ln(e + 1)$ where $e =$ engineering strain]

- (c) How can a pure metal be strengthened without changing the composition? Why cold working of tin (melting point 232°C) is not possible at room temperature?

- (c) In what way recrystallization is different from recovery? How do you distinguish between hot and cold working?

$$5 + 4 + 4 + 2 = 15$$

5. (a) The density of BCC Chromium is 7.19 g/cc. Find the lattice parameter if the atomic weight of the Cr is 54.01. [Given: 1 amu = 1.66×10^{-24} g]

- (b) Determine the magnitude of the Schmid factor for an FCC single crystal oriented with its [120] direction parallel to the loading axis.

- (c) Why do new phases usually nucleate in the grain boundaries of the prior unstable grains during solid-state transformations? What is significant about the magnitudes of the critical radii and the numbers of stable nuclei? Suggest microstructural feature of a fast cooled liquid.

- (d) For the solidification of nickel, calculate the critical radius r^* and the activation free energy ΔG^* if nucleation is homogeneous. Values for the latent heat of fusion and surface free energy are -2.53×10^9 J/m³ and 0.255 J/m², respectively. Degree of supercooling value for homogeneous nucleation and the melting point of Ni metal is 319 °C and 1450 °C, respectively.

Given:

$$r^* = \frac{-2\gamma T_m}{\Delta H_s(T_m - T)} = \frac{-2\gamma}{\Delta G_v}$$

$$\Delta G^* = \frac{16\pi\gamma^3}{3(\Delta G_v)^2}$$

$$4 + 3 + 4 + 4 = 15$$