

3.35 The landing gear of an airplane can be idealized as the spring-mass-damper system shown in Fig. 3.45. If the runway surface is described  $y(t) = y_0 \cos \omega t$ , determine the values of  $k$  and  $c$  that limit the amplitude of vibration of the airplane ( $x$ ) to 0.1 m. Assume  $m = 2000$  kg,  $y_0 = 0.2$  m, and  $\omega = 157.08$  rad/s.

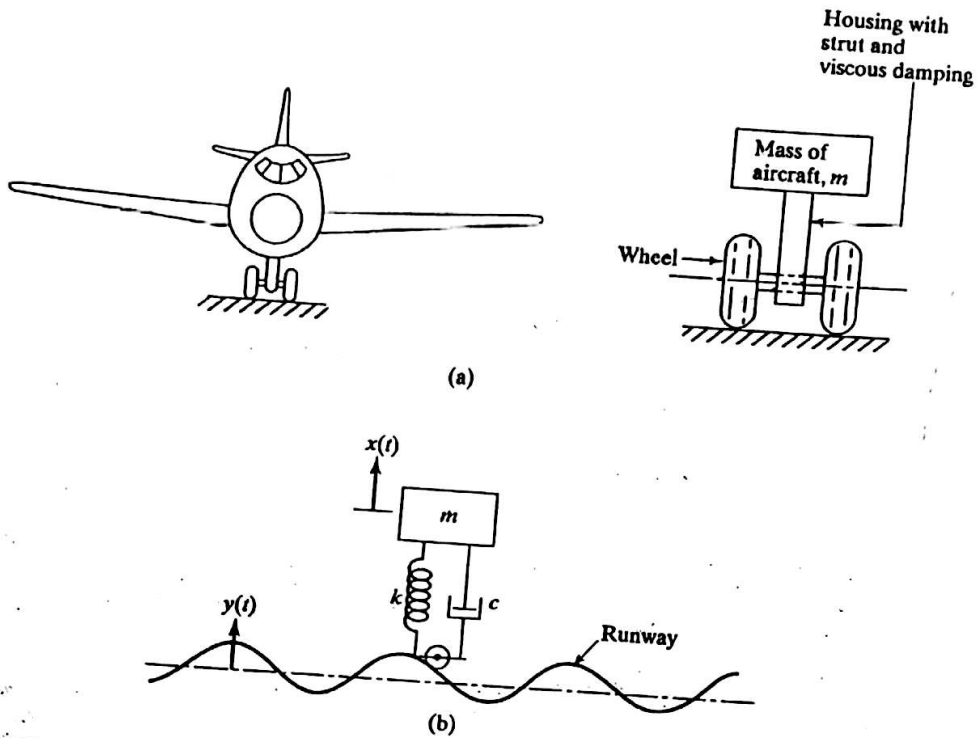


FIGURE 3.45 Modeling of landing gear.

3.37 Derive the equation of motion and find the steady-state response of the system shown in Fig. 3.47 for rotational motion about the hinge  $O$  for the following data:  $k = 5000$  N/m,  $l = 1$  m,  $c = 1000$  N-s/m,  $m = 10$  kg,  $M_0 = 100$  N-m,  $\omega = 1000$  rpm.

3.47 A uniform bar of mass  $m$  is pivoted at point  $O$  and supported at the ends by two springs, as shown in Fig. 3.52. End  $P$  of spring  $PQ$  is subjected to a sinusoidal displacement,  $x(t) = x_0 \sin \omega t$ . Find the steady-state angular displacement of the bar when  $l = 1$  m,  $k = 1000$  N/m,  $m = 10$  kg,  $x_0 = 1$  cm, and  $\omega = 10$  rad/s.

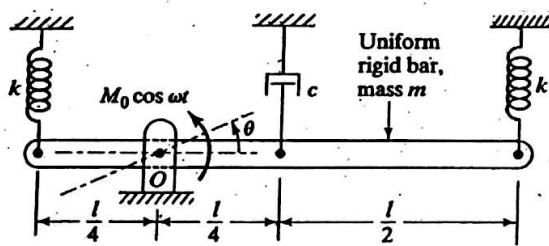


FIGURE 3.47

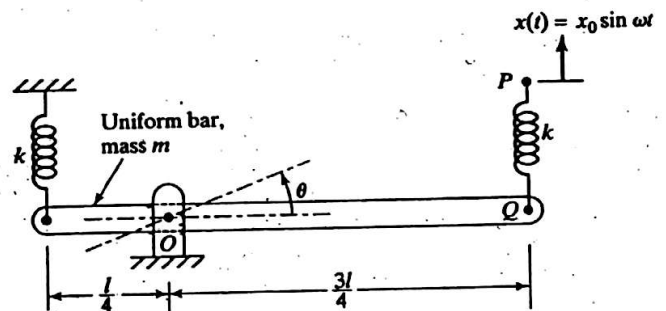


FIGURE 3.52

3.56 A centrifugal pump, weighing 600 N and operating at 1000 rpm, is mounted on six springs of stiffness 6000 N/m each. Find the maximum permissible unbalance in order to limit the steady-state deflection to 5 mm peak-to-peak.

# PROBLEMS ③

- 3.7 A spring-mass system consists of a mass weighing 100 N and a spring with a stiffness of 2000 N/m. The mass is subjected to resonance by a harmonic force  $F(t) = 25 \cos \omega t$  N. Find the amplitude of the forced motion at the end of (a)  $\frac{1}{4}$  cycle, (b)  $2\frac{1}{2}$  cycles, and (c)  $5\frac{3}{4}$  cycles.
- 3.8 A mass  $m$  is suspended from a spring of stiffness 4000 N/m and is subjected to a harmonic force having an amplitude of 100 N and a frequency of 5 Hz. The amplitude of the forced motion of the mass is observed to be 20 mm. Find the value of  $m$ .
- 3.11 An aircraft engine has a rotating unbalanced mass  $m$  at radius  $r$ . If the wing can be modeled as a cantilever beam of uniform cross section  $a \times b$ , as shown in Fig. 3.34(b), determine the maximum deflection of the engine at a speed of  $N$  rpm. Assume damping and effect of the wing between the engine and the free end to be negligible.

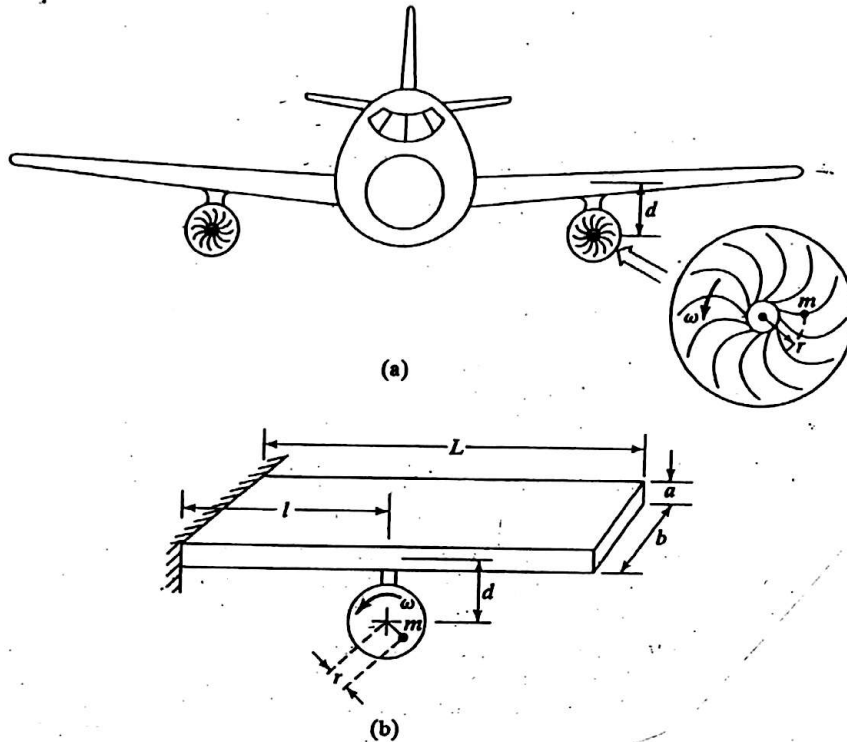


FIGURE 3.34

- 3.19 Derive the equation of motion and find the steady-state response of the system shown in Fig. 3.39 for rotational motion about the hinge  $O$  for the following data:  $k_1 = k_2 = 5000$  N/m,  $a = 0.25$  m,  $b = 0.5$  m,  $l = 1$  m,  $M = 50$  kg,  $m = 10$  kg,  $F_0 = 500$  N,  $\omega = 1000$  rpm.

- 3.20 Derive the equation of motion and find the steady-state solution of the system shown in Fig. 3.40 for rotational motion about the hinge  $O$  for the following data:  $k = 5000$  N/m,  $l = 1$  m,  $m = 10$  kg,  $M_0 = 100$  N-m,  $\omega = 1000$  rpm.

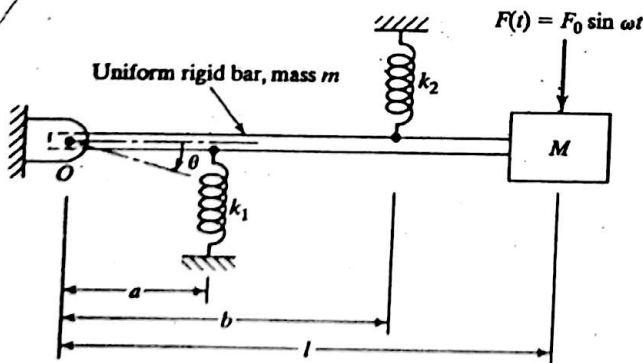


FIGURE 3.39

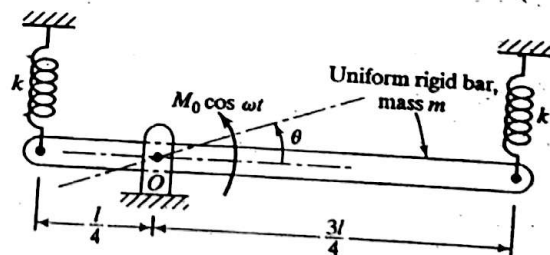


FIGURE 3.40

PTO