



BUSHED-PIN FLEXIBLE COUPLING

Power = 20 kW, N = 720 rpm,  $n_f = 2$

For Shaft

$P_1 = 1.5P$

$\Rightarrow P_1 = 1.5 \times 20 \text{ kW}$   
 $= 30 \text{ kW}$

$P_1 = T\omega$

$\Rightarrow T = \frac{30 \times 10^3}{720 \times \frac{2\pi}{60}} = 397.89 \text{ Nm}$

$\tau = \frac{0.5 S_{yt}}{2} = \frac{0.5 \times 300}{2} = 95 \text{ MPa}$

$\tau = \frac{16T}{\pi d^3} \Rightarrow d^3 = \frac{16 \times 397.89}{\pi \times 95 \times 10^6}$

$\Rightarrow d^3 = 2.133 \times 10^{-5} \text{ m}^3$

$\Rightarrow d = 27.73 \text{ mm (minimum)}$

$\therefore d \approx 30 \text{ mm}$  (from standard shaft size)

For Hub

$D = 2d = 2 \times 30 = 60 \text{ mm}$

$L = 1.5d = 1.5 \times 30 = 45 \text{ mm}$

$\tau = \frac{15}{2} \text{ MPa} = 7.5 \text{ MPa}$

$\tau = \frac{16TD}{\pi(D^4 - d^4)}$

$\Rightarrow \tau = \frac{16T}{\pi} \frac{2d}{(2d)^4 - d^4} = \frac{32Td}{\pi(15d^4)}$

$\Rightarrow \tau = \frac{32T}{15\pi d^3}$

$\Rightarrow d^3 = \frac{32}{15\pi} \cdot \frac{T}{\tau} = \frac{32}{15\pi} \times \frac{397.89}{7.5 \times 10^6}$

$\Rightarrow d = 33.02 \text{ (minimum)}$

So,  $d = 35 \text{ mm}$

$D = 2d = 70 \text{ mm}$

$L = 1.5d = 52.5 \text{ mm}$

For Key

$L = 1.5d = 52.5 \text{ mm}$

$\tau = \frac{0.5 \times 400}{2} = 100 \text{ MPa}$

$\tau = \frac{2T}{dWL}$

$W = \frac{2T}{dL\tau}$

$W = \frac{2 \times 397.89}{35 \times 10^{-3} \times 52.5 \times 10^{-3} \times 100 \times 10^6}$

$W = 4.33 \times 10^{-3} \text{ m}$

$\Rightarrow W = 4.33 \text{ mm (minimum)}$

$W = \frac{1}{4}d = \frac{1}{4} \times 35 = 8.75 \text{ mm}$

So,  $W = 9 \text{ mm}$

Now,  $\tau = \sigma_c$

$\Rightarrow \frac{2T}{dWL} = \frac{4T}{dhL}$

$\Rightarrow h = 2W$

$\therefore h = 2 \times 9 \text{ mm}$

$h = 18 \text{ mm}$

For Flange

$t_f = 0.5d = 0.5 \times 35 = 17.5 \text{ mm}$

$\tau_{max} = \frac{15}{2} = 7.5 \text{ MPa}$

$\tau = \frac{T}{\pi D t_f \times \frac{D}{2}}$

$\Rightarrow \tau = \frac{397.89}{\pi \times 70 \times 17.5 \times 35 \times 10^{-3}}$

$\Rightarrow \tau = 2.953 \text{ MPa}$

$\therefore \tau < \tau_{max}$

So,  $t_f = 17.5 \text{ mm}$

For rubber bushes and pins

$N = 6$

$105 \leq D_1 \leq 140$

$d_1 = 0.5d/\sqrt{N}$

$d_1 = 7.144 \text{ (pin diameter)}$

$D_1 = 3d$

$F = \frac{T}{N \left(\frac{D_1}{2}\right)} = \frac{397.89}{6 \times \frac{105}{2} \times 10^{-3}}$

$F = 1.263 \times 10^3 \text{ N}$

$\tau = \frac{F}{(\pi d_1^2/4)} = \frac{1.263 \times 10^3}{\pi \times \left(\frac{7.144}{4}\right)^2 \times 10^{-6}}$

$\tau = 31.5 \text{ MPa} \leq 35 \text{ MPa}$

$d_2 = d_1 + 2 \text{ mm} + 4 \text{ mm} + 12 \text{ mm}$   
 $= (7.144 + 2 + 4 + 12) \text{ mm}$

$\Rightarrow d_2 = 25.144 \text{ mm}$

$$l_2 = d_2$$

$$P_b = \frac{1.263 \times 10^3}{25.144 \times 25.144 \times 10^{-6}}$$

$$P_b = 1.997 \text{ MPa} > 1 \text{ MPa (Not Allowed)}$$

So, Taking  $D_1 = 4d = 140 \text{ mm}$

$$F = \frac{T}{N \frac{D_1}{2}} = \frac{397.89}{6 \times 70 \times 10^{-3}}$$

$$F = 0.9473 \times 10^3 \text{ N}$$

$$P_b = \frac{947.3}{(25.144)^2 \times 10^{-6}}$$

$$\Rightarrow P_b = 1.490 > 1 \text{ MPa (Not Allowed)}$$

So, Taking  $N=8$ ,  $D_1 = 4d = 140 \text{ mm}$

$$F = \frac{397.89}{8 \times \frac{140 \times 10^{-3}}{2}} = 710.52 \text{ N}$$

$$d_1 = 0.5 \times \frac{35}{\sqrt{8}} = 6.1871 \text{ mm}$$

$$d_2 = (6.1871 + 2 + 4 + 12) \text{ mm} \\ = 24.187 \text{ mm}$$

$$P_b = \frac{710.52}{(24.187)^2 \times 10^{-6}}$$

$$= 1.182 \text{ MPa} > 1 \text{ MPa (Not Allowed)}$$

So, Taking  $N=10$ ,  $D_1 = 4d = 140 \text{ mm}$

$$F = \frac{397.89}{10 \times \frac{140 \times 10^{-3}}{2}} = 568.41 \text{ N}$$

$$d_1 = 0.5 \times \frac{35}{\sqrt{10}} = 5.533 \text{ mm} \approx 6 \text{ mm}$$

$$d_2 = (6 + 2 + 4 + 12) \text{ mm} \\ = 24 \text{ mm}$$

$$l_2 = d_2 = 24 \text{ mm}$$

$$P_b = \frac{568.41}{(24)^2 \times 10^{-6}} \text{ Pa}$$

$$P_b = 0.9868 \text{ MPa} \leq 1 \therefore \text{Allowed}$$

$$\tau = \frac{F}{\frac{\pi d_1^2}{4}} = \frac{568.41}{\frac{\pi \times 6^2 \times 10^{-6}}{4}} = 20.1 \text{ MPa} \leq 35 \text{ MPa}$$

So,  $D_1 = 140 \text{ mm}$ ,  $N=10$ ,  $d_1 = 6 \text{ mm}$ ,  $d_2 = 24 \text{ mm}$

$$l_p = (l_2 + 5) \text{ mm} = 29 \text{ mm}$$

$$M = \frac{F l_p}{2} = \frac{568.41 \times 29 \times 10^{-3}}{2}$$

$$M = 8.241 \text{ Nm}$$

$$\therefore \sigma_b = \frac{M}{Z} = \frac{8.241 \times \frac{d_1}{2} \times \frac{32}{\pi d_1^4}}$$

$$= 8.241 \times \frac{6}{2} \times \frac{32}{\pi \times 6^4} \times 10^9$$

$$= 184.3 \text{ MPa}$$

$$\tau = 20.1 \text{ MPa}$$

$$\therefore \sigma_{\max} = \sqrt{\frac{\sigma_b^2}{4} + \tau^2}$$

$$= 99.2 \text{ MPa}$$