

SCHEMATIC DIAGRAM SHOWING THE SETUP.

# SHEAR AND BENDING IN BEAMS

## A. TRANSVERSE TEST

● Objective: To find the modulus of elasticity of the given specimen.

- Apparatus Required:
- ▶ 10 tons Universal Testing Machine (UTM)
  - ▶ dial gauge to measure deflections
  - ▶ scale or measuring tape

● Theory: An axis in the cross-section of a beam at half along which there is no longitudinal stress or strain is called Neutral axis. All layers on one side of the neutral axis are in a ~~state~~ state of tension while those on the opposite side are in compression. Radius of curvature of neutral surface of a beam subjected to pure bending, within elastic range is

$$\frac{1}{\rho} = \frac{M}{EI}$$

Radius of curvature is also  $\frac{1}{\rho} = \frac{d^2y/dx^2}{\left(1 + \left(\frac{dy}{dx}\right)^2\right)^{3/2}}$

neglecting  $\left(\frac{dy}{dx}\right)^2$ , we have

$$\frac{d^2y}{dx^2} = \frac{M}{EI}$$

● Observation Table

TABLE:1 LOADING

| LOAD<br>(KN) | DEFLECTION<br>(mm) |
|--------------|--------------------|
| 9.810        | 0.050              |
| 14.715       | 0.070              |
| 19.620       | 0.090              |
| 24.525       | 0.110              |
| 29.430       | 0.130              |
| 34.335       | 0.150              |
| 39.240       | 0.170              |
| 44.145       | 0.195              |
| 49.050       | 0.220              |
| 53.955       | 0.240              |
| 58.860       | 0.255              |
| 63.765       | 0.270              |
| 68.670       | 0.300              |

TABLE:2 UNLOADING

| LOAD<br>(KN) | DEFLECTION<br>(mm) |
|--------------|--------------------|
| 68.670       | 0.300              |
| 63.765       | 0.300              |
| 58.860       | 0.299              |
| 53.955       | 0.280              |
| 49.050       | 0.260              |
| 44.145       | 0.240              |
| 39.240       | 0.210              |
| 34.335       | 0.190              |
| 29.430       | 0.170              |
| 24.525       | 0.150              |
| 19.620       | 0.125              |
| 14.715       | 0.105              |
| 9.810        | 0.080              |
| 4.905        | 0.060              |
| 0            | 0.020              |

Boundary conditions for a simply supported beam is at  $x=0, y=0$  and at  $x=L, y=0$

We get maximum deflection  $y = \frac{PL^3}{48EI}$  where  $P = mg$

The maximum deflection is at the centre of the beam

$l \rightarrow$  length of unsupported beam

$I \rightarrow$  second moment of area about neutral axis

$$E = \frac{m'l^3}{bd^3}$$

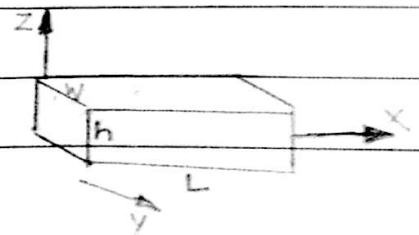
$m' \rightarrow$  slope of load vs. deflection graph

### ● Procedure:

- 1) Measured the dimensions of the specimen and held it on the supports on the UTM. Made sure that the specimen is symmetrically placed.
- 2) Mounted the dial gauge so that it touched the mid-section of the beam.
- 3) The motor was started and the load was applied gradually.
- 4) The values of load and corresponding deflection on the dial gauge was noted.
- 5) The care that the elastic limit is not exceeded was taken.

### ● Observation:

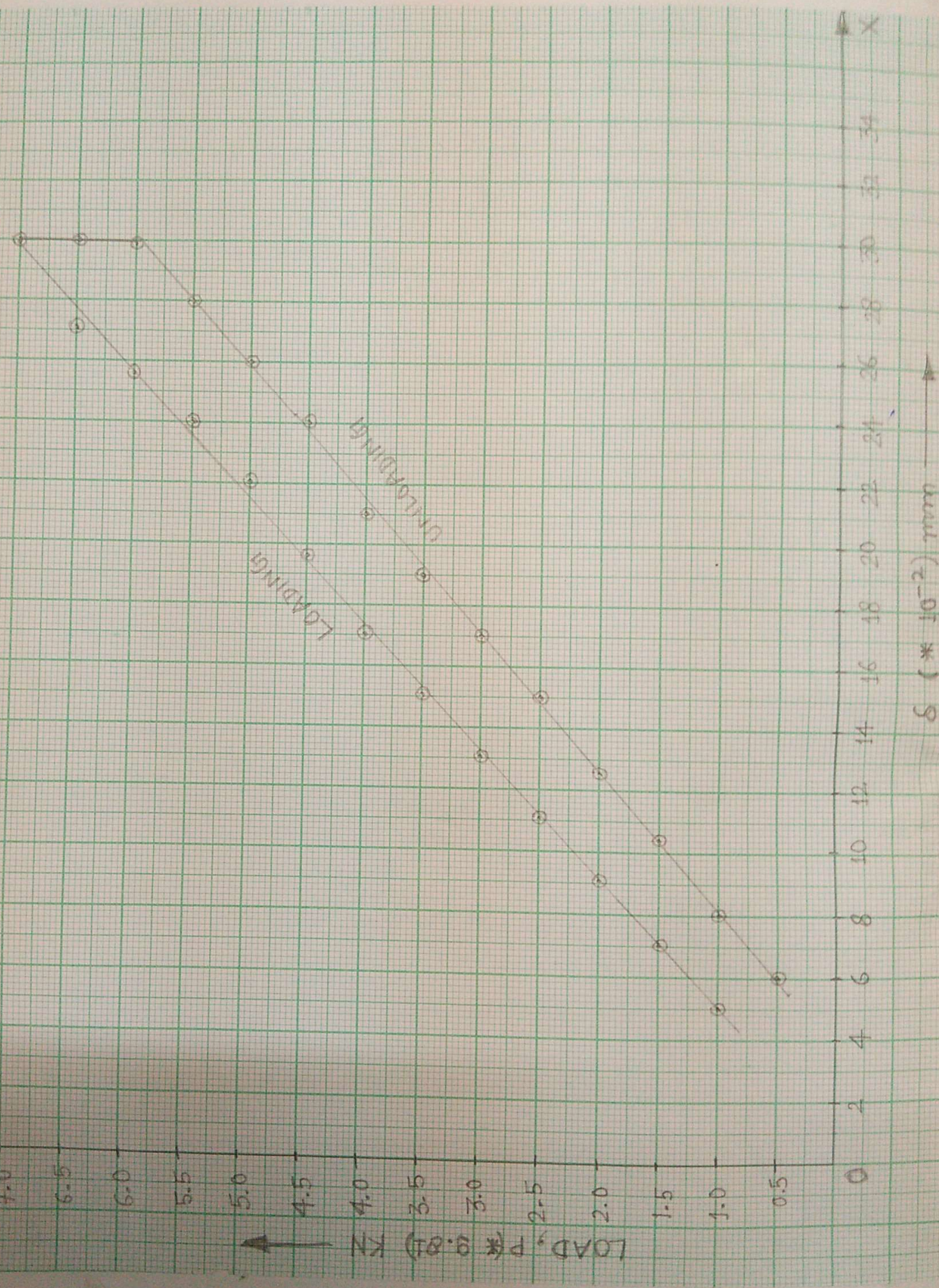
For the specimen, length = 300 mm  
height = 55 mm  
width = 55 mm





# PLOT between P and $\delta$

SCALE: On X axis, 1 cm = 0.02 mm  
 on Y axis, 1 cm = 4.905 kN





### Calculations:

$$I_y = \frac{1}{12} wh^3 = \frac{1}{12} \times 55 \times (55)^3 \text{ mm}^4$$

$$\Rightarrow I_y = 7.626 \times 10^5 \text{ mm}^4$$

calculating E for both loading and unloading at  $P = 29.43 \text{ kN}$

For loading  $\delta$  at  $29.43 \text{ kN} = 0.13 \text{ mm}$

$$\therefore E_1 = \frac{29.43 \times 10^3 \times (300)^3 \times (10^{-3})^3}{48 \times 0.13 \times 10^{-3} \times 7.626 \times 10^5 \times (10^{-3})^4} \text{ N/m}^2$$

$$= 16.7 \times 10^{10} \text{ N/m}^2$$

$$E_1 = 167 \text{ GPa}$$

For unloading,  $\delta$  at  $29.43 \text{ kN} = 0.17 \text{ mm}$

$$\therefore E_2 = \frac{29.43 \times 10^3 \times (300)^3 \times (10^{-3})^3}{48 \times 0.17 \times 10^{-3} \times 7.626 \times 10^5 \times 10^{-12}} \text{ N/m}^2$$

$$= 12.769 \times 10^{10} \text{ N/m}^2$$

$$E_2 = 127.69 \text{ GPa}$$

$$\therefore E_{\text{average}} = \frac{E_1 + E_2}{2}$$

$$E_{\text{average}} = 147.345 \text{ GPa}$$

### Result:

The average value of E is 147.345 GPa.

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### Discussions:

- The load should show linear relationship with displacement and our plot of load vs displacement shows the linear

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relationship too.

➤ From the table,  $E_{\text{mild steel}} = 205 \text{ GPa}$

$$\therefore \% \text{ error} = \frac{205 - 147.345}{205} \times 100\%$$

$$= 28.124\%$$

## SHEAR AND BENDING IN BEAMS.

### B. SHEAR TEST

① Objective: To find the shear strength of the given material.

② Apparatus Required:   
 ▶ 10 tons Universal Testing Machine (UTM)   
 ▶ Shear Test attachments and specimen.   
 ▶ Micrometer.

③ Specifications: In this experiment, the specimen provided was subjected to double shear. This increases the load which it can withstand. Bolts are often used in double shear thus increasing safety.

Breaking load =  $P$  (found from experiment)

$$\text{Shear strength} = \frac{P}{2A}$$

$A \rightarrow$  Area of cross section.

④ Procedure:

- 1) Measurement of the diameter of the specimen using micrometer was taken.
- 2) The specimen was fitted in the shearing attachments.
- 3) The shearing attachments onto the UTM were installed.
- 4) The motor was started and the load was applied gradually.
- 5) The load was increased upto the failure of the specimen due to shear.



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6) The load reading was noted down when the specimen got sheared off.

① Observations and calculations:

$$d_{\text{top}} = 9.40 \text{ mm}$$

$$d_{\text{bottom}} = 9.40 \text{ mm}$$

$$d_{\text{middle}} = 9.47 \text{ mm}$$

$\therefore$  Diameter of the specimen,  $d = 9.423 \text{ mm}$  (Average)

$$\text{Cross sectional area} = \frac{\pi d^2}{4} = \frac{\pi \times (9.423)^2}{4} \text{ mm}^2$$

$$= 69.738 \text{ mm}^2$$

$$\therefore \text{Shear strength} = \frac{P}{2A}$$

Here, Break load,  $P = 66.46275 \text{ KN}$

$$\therefore \text{Shear strength} = \frac{66462.75}{2 \times 69.738} \frac{\text{N}}{\text{mm}^2}$$

$$= 476.517 \frac{\text{N}}{\text{mm}^2}$$

$$= 476.517 \text{ MPa}$$

① Result:

The value of shear strength as obtained from the experiment is 476.517 MPa

① Discussions:

- For shear test, the shear load was double shear. Thus the load acting on each of the shear planes is  $P/2$ .
- The load should not be increased after fracture or even after yielding starts in the material.